

2010

B. Engg. (Mechanical Engg.)-6th Semester
MEC-602: Finite Element Methods

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Q. No. 1 which is compulsory and selecting two questions from each Section-I & II. Make suitable assumptions wherever applicable.

- *_ *_ *

Q1: Briefly answer the following questions. (1 x 10 = 10)

- With the help of a figure, briefly explain Saint Venant's principle.
- A bar element with two nodes is placed in 3D. How many and what kind of dofs are present there?
- State the principle of minimum potential energy.
- What are major disadvantages of finite element methods?
- What are important rules for placing nodes in a finite element model?
- With the help of a figure show the characteristics of a constant strain triangle (CST)?
- Show the characteristics of a two dimensional frame element with the help of a figure.
- What do you understand by topology optimization?
- What are the advantages of Galerkin approach in FEM?
- What is Guyen's reduction?

Section-I

Q2: (a) A system of springs is shown in the figure 1. Find out the extension at its nodes using either the direct approach or the potential energy approach. (5)

(b) A bar is fixed from two ends as shown in the figure 2. Using an approximate displacement function $u = a_1 + a_2 \cdot x + a_3 \cdot x^2$, find out the displacement and stress along the x-axis. (5)

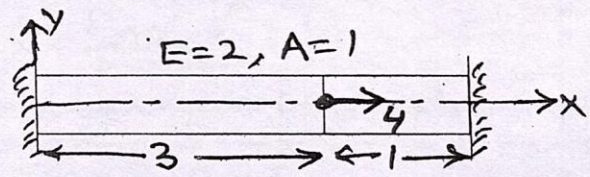
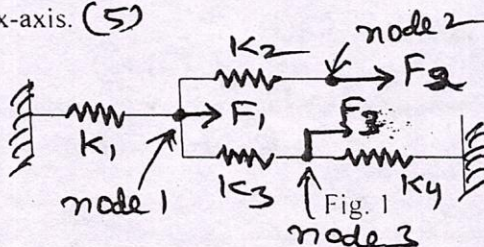


Fig. 2

Q3: (a) A stepped bar is shown in the figure 3. Using a suitable finite element method, find the displacement, element stresses and reaction at its nodes. (8)

(b) Briefly explain quadratic shape functions. (2)

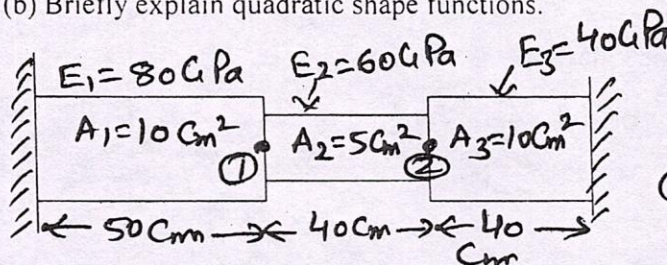


Fig. 3

Force at node 1 = 100 kN (+x)
node 2 = 60 kN (+x)

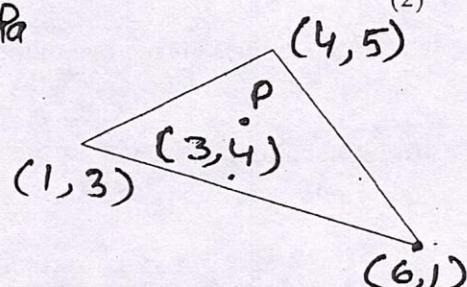


Fig. 4

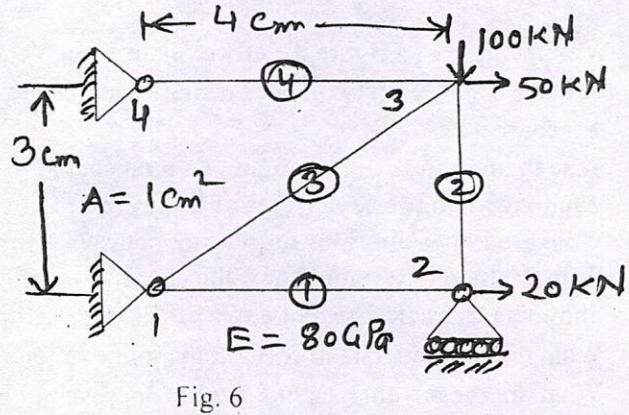
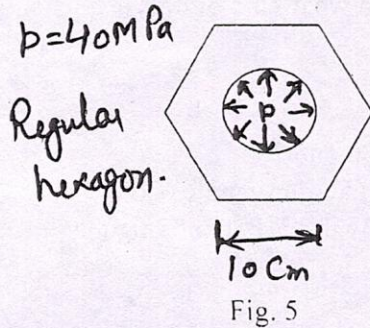
P.T.O.

(2)

Q4: (a) A point P lying within the triangular element shown in the figure 4. Find out its shape functions. Also find out the displacement at the point P given that the displacement at node 1, 2 and 3 is (0.1, 0.2), (0.1, 0.1) and (0.2, 0.1) respectively. (5)

(b) Draw an axisymmetric element having triangular sweeping area and indicate degrees of freedom on it. (2)

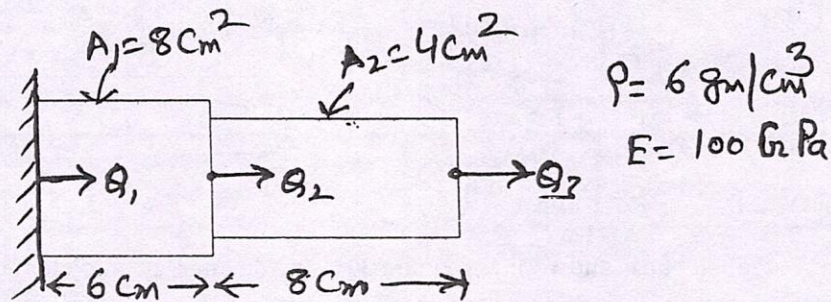
(c) A hexagonal plate lying in x-y plane is subjected to internal stresses as shown in the fig. 5. Simplify the model and also apply suitable boundary conditions on it. (3)



Section II

Q5: A two dimensional truss as shown in the fig. 6. Find out the nodal displacements. Also find out the element stresses in element 2 and 3. Also find out the reactions at node 1. (10)

Q6. A problem shown in the figure 7, find out the eigen values and eigen vectors. (10)



Q7: Write short notes on any two of the following

5 x 2 = 10

- (a) Rigid body modes
- (b) Structural optimization
- (c) Finite element in design