

2015

B.E. (Mechanical Engineering)

Fourth Semester

MEC-402: Mechanics of Solids

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part. Use usual notations and symbols for derivations. Assume suitably missing data if any. All questions carry equal marks.

x-x-x

Q.1 Provide brief and clear answers to the following:

- Give the expression for shear stress in a closed thin walled tube under torsion.
- What is the value of moment of inertia when the product of inertia is zero.
- Write the expression for the eccentricity of the neutral axis for a curved beam in pure bending.
- Provide the expression for the complementary energy for a linear elastic cable.
- Write the expression between critical stress and slenderness ratio.

Part A

Q.2 Strains for a state of plane stress are given by $\epsilon_x = -90\mu$, $\epsilon_y = -30\mu$, and $\gamma_{xy} = 120\mu$. If the elastic constants for the structure are $E = 209 \text{ GPa}$ and $\nu = 0.29$, determine the complete strain and stress matrices.

Q.3 Determine the stress fields that arise from the following stress functions:

$$\Phi = Cy^2,$$

$$\Phi = Ax^2 + Bxy + Cy^2,$$

$$\Phi = Ax^3 + Bx^2y + Cxy^2 + Dy^3,$$

where A , B , C , and D are constants. Also suggest what states of stress the functions are suitable for. In addition check if the compatibility is satisfied.

Q.4 Determine the stress distribution in a thick walled cylinder with an inner diameter of 50mm and outer diameter of 150mm with $p_i = 35 \text{ MPa}$ and $p_o = 0$.

Part B

Q.5 Consider a cantilever beam of length $L = 1 \text{ m}$ with a concentrated load $P = 500 \text{ N}$ applied at a distance $b = 0.2 \text{ m}$ from the free end. Taking the stiffness of the beam $EI = 10 \times 10^4 \text{ N-m}^2$, determine the vertical deflection of the free end.

Q.6 Estimate the torque on a 10mm diameter steel shaft when yielding begins using (a) the Tresca and (b) the von Mises theory. The yield strength of steel is 140MPa.

Q.7 A three element rectangular rosette strain gage is mounted on a steel specimen. For a particular state of loading of the structure the strain gage readings are $\epsilon_A = 200\mu$, $\epsilon_B = 900\mu$, and $\epsilon_C = 1000\mu$. Determine the values and orientations of the principal stresses and the value of the maximum shear stress at the point. Let $E = 200 \text{ GPa}$ and $\nu = 0.285$.

x-x-x