

2125
B.E. (Computer Science and Engineering)
Fifth Semester
CS-504: Theory of Computation

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Section.

x-x-x

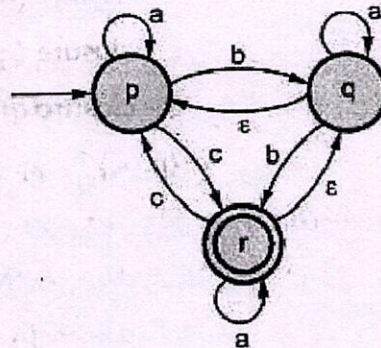
1. Answer the following:

- Differentiate between Mealy and Moore machines.
- Construct a DFA accepting the language over the alphabet $\{0, 1\}$ that has the set of all strings ending in '00'.
- What is Kleene's closure? Find $a(a)^*$.
- Show that the grammar $S \rightarrow SbS | a$ is ambiguous.
- Give the formal definition of acceptance by PDA.
- Explain Instantaneous description of Turing Machine by taking its snapshot.
- Find the derivation tree for a grammar, $G: S \rightarrow 0B | 1A, A \rightarrow 0 | 0S | 1AA, B \rightarrow 1 | 1S | 0BB$ for the string 00110101.
- Describe Multi-tape Turing machine.
- Define NP and P classes.
- Let G be $S \rightarrow AB, A \rightarrow a, B \rightarrow C | b, C \rightarrow D, D \rightarrow E$ and $E \rightarrow a$. Eliminate unit productions and get an equivalent grammar.

(10x1=10)

Section A:

2. a) Construct a deterministic finite automaton which is equivalent to nondeterministic finite automata with ϵ -moves whose transition diagram is given below.



- b) Consider the transition table given below. Prove that the strings recognized are $(a + b(b + abb)^*(aa + aba))^*(b(b + abb)^*ab)$.

Σ	a	b
Q		
$\rightarrow q_1$	$\{q_1\}$	$\{q_2\}$
q_2	$\{q_3\}$	$\{q_2\}$
q_3	$\{q_1\}$	$\{q_4\}$
$\odot q_4$	$\{q_1\}$	$\{q_2\}$

(06+04)

3. a) Construct the reduced grammar equivalent to the grammar $G = (\{U, V, W, X, Y, \}, \{0, 1\}, P, U)$, where the set of productions P is given as follows:
 $U \rightarrow 0V0$
 $V \rightarrow U1 | 1WW | Y0V$
 $W \rightarrow 011 | YY$
 $X \rightarrow 0W$
 $Y \rightarrow 0YV$

P.T.O.

(2)

- b) Convert the grammar $G = (\{X, Y, Z\}, \{0, 1\}, P, X)$, into Greibach normal form, where the set of productions P is given as follows:

$X \rightarrow YZ$
 $Y \rightarrow ZX|1$
 $Z \rightarrow XY|0$

(04+06)

4. a) Find a regular expression that represents all binary strings over $\{0,1\}$ containing an even number of 1s. Convert the regular expression into nondeterministic finite automata with ϵ -moves and then into the corresponding deterministic finite automata.
 b) Define distinguishable and indistinguishable states. Construct a minimum state Automaton equivalent to a DFA whose transition table is given below. Draw the transition diagram of resulting DFA.

Σ Q	0	1
$\rightarrow q_0$	q_1	q_4
q_1	q_2	q_5
(q_2)	q_3	q_7
q_3	q_4	q_7
q_4	q_5	q_8
(q_5)	q_6	q_1
q_6	q_7	q_1
q_7	q_8	q_2
(q_8)	q_0	q_4

(04+06)

Section B:

5. a) Construct pushdown automata for accepting the language $L = \{WW^R \mid W \text{ in } (0+1)^*\}$.
 b) Construct a CFG which accepts $N(A)$ where $A = (\{q_0, q_1\}, \{a, b\}, \{Z_0, Z\}, \delta, q_0, Z_0, \emptyset)$. δ is given by:

$\delta(q_0, b, Z_0) = \{(q_0, ZZ_0)\}$
 $\delta(q_0, \wedge, Z_0) = \{(q_0, \wedge)\}$
 $\delta(q_0, b, Z) = \{(q_0, ZZ)\}$
 $\delta(q_0, a, Z) = \{(q_1, Z)\}$
 $\delta(q_1, b, Z) = \{(q_1, \wedge)\}$
 $\delta(q_1, a, Z_0) = \{(q_0, Z_0)\}$

(05+05)

6. a) Discuss in detail the halting problem and its consequences.
 b) Design a Turing machine that can accept the set of all even palindromes over $\{0, 1\}$. Draw its transition diagram also. Compute the sequence of execution by taking suitable string of given language.

(03+07)

7. a) Discuss in detail Tractable and Intractable problems.
 b) Explain why one should study undecidability?
 c) Let f be the function $f(n) = n - 1$ when $n > 0$ and $f(0) = 0$. Show that f is computable.

(03+03+04)