

2124

M.E. (Computer Science and Engineering)
First Semester
CS-8101: Advance Algorithms
(Common with CSN 8101)
(For UIET)

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 (Section-A) which is compulsory and selecting two questions from each Section B-C.

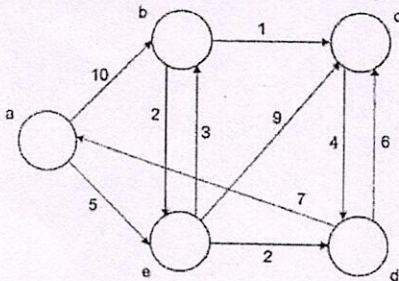
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Section-A

- Q1 (a) Why do we should not look only at worst case analysis? What are different methods for analyzing recurrence algorithms? (2)
- (b) What are different methods for analyzing recurrence algorithms? (2)
- (c) Given the following functions $f_1 = \log(n!)$, $f_2 = (\log n)!$, $f_3 = n^{\log(n)}$, $f_4 = \log(\log(n))$. Arrange these functions in increasing order of their growth. (2)
- (d) What is the difference between NP hard and NP complete problems? (2)
- (e) What is the time complexity of string matching with finite automata and compare it with the naïve string matching algorithm. (2)

Section-B

- Q2 (a) Discuss the correctness of following equalities (5)
- (i) $n! = O(n^n)$
- (ii) $2^n + n \log n + 5 = \theta(n^3)$
- (b) Solve the recurrence relation $T(n) = 4T\left(\frac{n}{2}\right) + \theta(n^2)$ is (5)
- Q3 (a) Explain the strassen's matrix multiplication algorithm in detail. Compare its time complexity with other matrix multiplication algorithms. (5)
- (b) Explain Prim's algorithm and describe the data structures used in its implementation. List the costs of the edges of following graph in the order chosen by it. (5)



- Q4 (a) Discuss the significance of Lower Bound theory for algorithm designers. Draw the comparison tree for binary search. Prove that minimum comparisons required for any comparison-base algorithm on n-elements is more than $\log(n+1)$. (5)
- (b) Discuss the greedy method to solve the knapsack problem for instance $n=7$, $m=15$, $(P_1, P_2, \dots, P_7) = (10, 5, 15, 7, 6, 18, 3)$ and $(W_1, W_2, \dots, W_7) = (2, 3, 5, 7, 1, 4, 1)$. Is this the optimal method? (5)

Section-C

- Q5 (a) State the principal of optimality. How dynamic programming is different from the greedy programming? Write an algorithm to solve Traveling Salesman problem using Dynamic Programming. (5)
- (b) Define Multistage Graph and discuss an algorithm to find the cost path from source to sink using dynamic programming (5)
- Q 6(a) Using the text $T = \text{"ABABABCABABABAC"}$ and the pattern $P = \text{"ABABAC"}$, demonstrate the execution of the KMP algorithm step-by-step. Show how the partial match table is used to skip unnecessary comparisons. (5)
- (b) Design a PRAM algorithm to color the graph $G=(V,E)$ with n vertices and m edges using the minimum number of colors such that no two adjacent vertices share the same color. (5)
- Q 7 a) What are the main steps for designing an approximation algorithm? Which one is better: n -approximation, $\log n$ -approximation, \sqrt{n} -approximation, constant factor approximation (5)
- (b) What are NP-Scheduling problems? Explain and compare them with NP-hard and NP-complete problems. (5)

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