

2053  
B.E. (Mechanical Engineering)  
Eighth Semester  
MEC-803: Computational Fluid Dynamics

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Section. All questions carry equal marks.

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1. (a) What are the important applications of CFD in engineering?
- (b) Distinguish between conservation and non-conservation forms of fluid flow.
- (c) What are the different categories of boundary conditions? Give example of each category.
- (d) Compare implicit and explicit methods.
- (e) Discuss the need of upwind type discretization. (5×2)

SECTION-A

2. (a) Compare the merits and demerits of experimental fluid dynamics, theoretical fluid dynamics and computational fluid dynamics.
- (b) Derive the x-momentum equation for unsteady 3-dimensional flow. (5+5)
3. (a) Define and develop expression for substantial derivative. (3 + 7)
- (b) Explain the different models of fluid flow with derivation of continuity equation.
4. (a) Classify the following system of PDEs according to eigen value method:  
$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0; \quad \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} = 0, \text{ where } u, v \text{ are dependent variables.}$$
- (b) Prove that second order wave equation:  $\frac{\partial^2 u}{\partial t^2} = \frac{\partial^2 u}{\partial x^2}$  is hyperbolic.
- (c) Write a note on well-posed and ill-posed problems. (5 + 2 + 3)

SECTION-B

5. (a) Derive the finite difference expressions for a first and second order derivatives with forward, backward and central difference approximations using Taylor series expansion with the leading error term. (3 + 3 + 4)
- (b) Distinguish between rounding off error, truncation error and discretization error.
- (c) Consider 1-dimensional wave equation  $\frac{\partial u}{\partial t} + a \frac{\partial u}{\partial x} = 0$ . Discretize the equation and hence deduce dissipative term and dispersive term.
6. (a) Discuss finite volume method for 1-D and 2-D diffusion problems.
- (b) Compare upwind and central difference approximations for convection-diffusion problems. (5+5)
7. (a) Explain SIMPLE algorithm. Compare SIMPLE and SIMPLER algorithms.
- (b) What is Tri-diagonal matrix algorithm (TDMA)? Why it is used? Explain the algorithm in detail. (5+5)