

2053  
B.E. (Mechanical Engineering)  
Fourth Semester  
MEC-404: Numerical Analysis

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each section. Use of simple calculator is allowed. All questions carry equal marks.

x-x-x

1. (a) Consider the number 52.43, which is correct to four significant figures. Find absolute error, relative error and percentage error.
- (b) State Newton's formula to find a root of  $f(x) = 0$ . Why this method is also known as method of tangents? Write down its merits and demerits.
- (c) What is the Lagrange's formula to find  $y$ , if  $(x_0, y_0), (x_1, y_1), (x_2, y_2)$  are given?
- (d) Write down the Euler's and modified Euler's method to solve:  
$$\frac{dy}{dx} = f(x, y), y(x_0) = y_0.$$
 Explain the difference between them.
- (e) Approximate  $4x^3 + 2x^2$  using Chebyshev polynomial.

SECTION-A

2. (a) Find the number of term of the exponential series such that their sum gives sum of  $e^x$  correct to nine decimal places at  $x = 1$ .
- (b) Find a root of the equation  $x - \cos x = 0$  by using the Bisection method correct to three decimal places. Find the number of iterations required to achieve this such accuracy.
3. (a) Find a positive root of the equation  $3x - \cos x - 1 = 0$  by Newton method.
- (b) Define forward, backward and shift operators. Derive the relation between them. Find the missing values in the following data using them:  

$x:$	0	5	10	15	20	25
$f(x):$	6	10	-	17	-	31
4. (a) Using Newton's divided difference formula, evaluate  $f(8)$  and  $f(15)$  from the following data:  

$x:$	4	5	7	10	11	13
$f(x):$	48	100	294	900	1210	2028
- (b) Find the value of  $x$  if  $\sqrt[3]{x} = 3.756$  given the following data:

$x$	50	52	54	56
$f(x)$	3.684	3.732	3.779	3.825

(2)

## SECTION-B

5. (a) Solve the following equations by Gauss elimination method:

$$x + 4y - z = -5; \quad x + y - 6z = -12; \quad 3x - y - z = 4.$$

(b) Find the smallest eigenvalue of the matrix  $A = \begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$  by using inverse power method.

6. (a) Compute  $\int_0^1 \frac{x}{x^3+10} dx$  with 9 ordinates by Trapezoidal and Simpson's one-third rule.

(b) Given  $\frac{dy}{dx} = 3x + y^2$ , where  $y(1) = 1.2$ . Use Runge-Kutta method of second order to find approximate value of  $y(1.1)$  correct to three decimal places.

7. (a) Using the finite difference method, find  $f(0.25)$ ,  $f(0.5)$  and  $f(0.75)$  satisfying the differential equation:  $\frac{d^2y}{dx^2+y} = x$  subject to  $y(0) = 0, y(1) = 2$ .

(b) Economize the series given by  $\sinh x = x + \frac{x^3}{6} + \frac{x^5}{120} + \frac{x^7}{5040} + \dots$  on  $[-1, 1]$ , allowing for a tolerance of 0.0005.