

2063

**B.E. (Computer Science and Engineering)**  
**Third Semester**  
**CS-303: Discrete Structures**

Time allowed: 3 Hours

Max. Marks: 50

**NOTE:** Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Section.

x-x-x

1. Briefly explain the following with example:

- (a) Reflexive and Irreflexive relations
- (b) K-Regular graph
- (c) Monoid
- (d) Recurrence relation
- (e) Quantifiers

(5x2=10)

**Section-A**

2. (a) Consider the universal set  $U=\{1,2,3,4,\dots,10\}$  and the subsets  $A=\{1,7,8\}$ ,  $B=\{1,6,9,10\}$ ,  $C=\{1,9,10\}$ . List the non-empty minsets and maxsets generated by A, B and C. Do the minsets and the maxsets form a partition of U? (4)
- (b) Let R be a relation defined on the set of positive integers such that for all  $x,y \in \mathbb{Z}^+$ ,  $xRy$  if and only if  $|x-y|<7$ . Determine whether R is an equivalence relation. (4)
- (c) Is the Implication and its inverse logically equivalent? Justify your answer. (2)
3. (a) Show that the mapping  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = ax + b$ , where  $a, b, x \in \mathbb{R}$ ,  $a \neq 0$  is invertible. Find its inverse. (4)
- (b) Prove that there is no largest integer that is a multiple of 5 using a suitable method of proof. (3)
- (c) Show that  $\forall x(P(x) \vee Q(x)) \Rightarrow \forall xP(x) \vee \exists xQ(x)$ . (3)
4. (a) Let  $D_{100} = \{1, 2, 4, 5, 10, 20, 25, 50, 100\}$  whose all the elements are divisors of 100. Let the relation  $<$  be the relation  $|$  (divides) be a partial ordering on  $D_{100}$ .
  - I. Draw the Hasse diagram of the given poset.
  - II. Determine the glb of  $\{10,20\}$  and  $\{5,10,20,25\}$
  - III. Determine the lub of  $\{10,20\}$  and  $\{5,10,20,25\}$  (5)
- (b) Show the implication  $p \rightarrow q \Rightarrow p \rightarrow (p \wedge q)$  without using truth table. (3)
- (c) Let R be a binary relation on A such that  $(a, b) \in R$ , if book 'a' costs more and contains fewer pages than book 'b'. Is R an Equivalence Relation or a Partial Order Relation? Justify. (2)

P.T.O.

(2)

**Section-B**

5. (a) Prove that total number of permutations of  $n$  different things taken not more than  $r$  at a time, when each thing may be repeated any number of times is  $n(n^r-1)/(n-1)$ . (5)
- (b) Consider  $a \in \mathbb{R}$  as a constant real number. Assume  $G = \{a^n: n \in \mathbb{Z}\}$ . Prove that  $G$  is an abelian group under usual multiplication. (5)
6. (a) Solve the recurrence relation  $a_r + 5a_{r-1} + 6a_{r-2} = 3r^2$ . (6)
- (b) Define order and size of a graph. Describe Complement and Subgraph of a graph giving examples. (4)
7. (a) Discuss the Breadth-First Traversal technique using a suitable example. (6)
- (b) Define an algebraic structure. Differentiate between a ring and a field. (4)

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