

2023

M. Tech. (Material Science and Technology)

First Semester

MT-102: Quantum Physics in Atoms and Molecules

Time allowed: 3 Hours

Max. Marks: 50

**NOTE:** Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part.

x-x-x

1. Attempt the following: (This question is compulsory)

(2x5=10)

- Why can't we observe Compton effect with visible light?
- Show that Quantum mechanical Harmonic oscillator problem is in accord with Correspondence principle.
- On what factors does thermionic emission from any metal depends?
- What is the difference between ab-initio methods and DFT?
- Compare the ground state momentum of the particle in the two potential wells having same width such that one of the wells has finite height and other has infinite height.

#### PART A

- What are the salient features of Black body radiation spectrum? Show that R-J law failed but Planck's distribution law explains the blackbody radiation spectrum. (6)
  - What effect on the scattering angle in the Davisson Germer experiment does increasing the electron energy have? (2)
  - In an experiment, tungsten cathode, which has a threshold wavelength  $2300\text{\AA}$ , is irradiated by ultraviolet light of wavelength  $1800\text{\AA}$ . Calculate the maximum energy of emitted photoelectrons and work function of tungsten. (2)
- Establish the time dependent and time independent form of Schrodinger equation. (5)
  - Using Uncertainty Principle, show that electrons cannot reside inside the nucleus. (2)
  - What are matter waves? Show that matter waves travel with the velocity of the body. (3)
- Show that there is a finite probability of finding the particles across the barrier even if the energy of particles  $E$  is less than barrier height. Also, determine the flux of incident particles, reflected particles, and the particles transmitted. Also plot the behaviour of wavefunction in various regions of barrier. (6)
  - A particle limited to  $x$  axis has the wave function  $\psi = ax$  between  $x = 0$  and  $x = 1$ ;  $\psi = 0$  elsewhere. Find the expectation value of  $x$ . (2)
  - Find the commutator  $[x, H]$ . (2)

#### PART B

- Give basic postulates of free electron theory and tell what modifications have been considered in Kronig Penney (K-P) Model to remove the failures of classical free electron theory. Show that if  $V = 0$ , the energy spectrum proposed by K-P model becomes continuous and it is that of the free particle. Use physical arguments to justify this result. (7)
  - Explain how resistivity of metals varies with composition and temperature. (3)
- Derive an expression for effective mass? Discuss its variation and that of group velocity in a band. (5)
  - Discuss briefly the various theoretical models proposed to understand the specific heat of solids, citing clearly the basic assumptions and limitations of the models if any. (3)
  - Calculate the relaxation time of electron in sodium if the Fermi energy of sodium is  $3.1\text{ eV}$  and electrical conductivity is  $2.1 \times 10^7\text{ S/m}$  at  $0\text{ K}$ . (2)
- What is Born Oppenheimer approximation? How does it simplify Schrodinger many body equation? (5)
  - What do you mean by Local density approximation in DFT? How is it different from GGA? Give the name of any two software codes based on DFT. (5)

x-x-x