Exam.Code:0940 Sub. Code: 7049

## 1059

## B.E. (Mechanical Engineering) Fourth Semester MEC-404: Numerical Analysis

Max. Marks: 50

Attempt <u>five</u> questions in all, including Question No. I which is compulsory and selecting two questions from each Section. Use of simple calculator is allowed.

x-x-x

- 1 (a) Explain fixed point method. What is the condition for the convergence of fixed point iteration method? Find its order of convergence.  $(5 \times 2 = 10)$
- (b) State Newton's forward and backward interpolation formulas.
- (c) What is the use of power method? Explain.
- (d) State Romberg's integration formula to find the value of  $I = \int_a^b f(x) dx$  for first two intervals. Why it is better than trapezoidal formula?
- (e) Obtain the finite difference scheme for the differential equation: 2y''(x) + y(x) = 5.

## SECTION-A

- II. (a) Write a note on error propagation and numerical instability. Find the number of terms of the exponential series such that their sum gives the value of  $e^x$  correct to six decimal places for all values of x in  $0 \le x \le 1$ .
- (b) Prove that the Regula-falsi method has linear order of convergence whereas secant method is super-linearly convergent. Explain, why?
- III. (a) Find the quadratic factor of  $f(x) = x^3 2x^2 + x 2$  by Lin-Bairstow's method.
- (b) Using Newton divided difference formula, find f(x) as a polynomial in powers of (x-3):  $\begin{cases} x: & 5 & 11 & 27 & 34 & 41 \\ f(x): & 23 & 899 & 17315 & 15600 & 68510 \end{cases}$
- IV. (a) How Lagrange's formula can be used to express the rational function as a sum of partial fractions. Express  $f(x) = \frac{x^2 + x 3}{x^3 2x^2 x + 2}$  as a sum of partial fractions.
  - (b) Explain inverse interpolation. Values of x and  $e^x$  are given below:

(1.4, 4.0552), (1.5, 4.4817), (1.6, 4.9530), (1.7, 5.4739). Find x when  $e^x = 4.7115$ , using the method of successive approximations.

## **SECTION-B**

V. (a) Solve the following system of linear equations using Gauss-Seidel method:

$$x+4y+z=6$$
,  $x+y+4z=6$ ,  $4x+y+z=6$ 

(b) Reduce the matrix to the tri-diagonal form by Householder's method:

$$A = \begin{bmatrix} 1 & 3 & 4 \\ 3 & 2 & -1 \\ 4 & -1 & 1 \end{bmatrix}.$$

VI. (a) State Gerschgorin and Brauer theorems. Estimate the eigenvalues of the matrix and plot them:  $A = \begin{bmatrix} 5 & 1 & 1 \\ 0 & 6 & 1 \\ 1 & 0 & -5 \end{bmatrix}$ .

- (b) Compute  $I = \int_{-1}^{1} \frac{1}{x^2 + 1} dx$  using trapezium and Simpson's one-third rules by taking eight equal intervals.
- VII. (a) Solve the boundary value problem using finite difference method:  $\frac{d^2y}{dx^2} + y + x = 0, 0 < x < 1, y(0) = y(1) = 0.$
- (b) Find the economized power series for  $\cos x = 1 \frac{x^2}{\angle 2} + \frac{x^4}{\angle 4} -$  for  $0 \le x \le 1$  with a tolerance of  $\varepsilon = 0.02$ . (4+4+2)
- (c) Find the best lower order approximation to cubic polynomial:  $5x^3 + 4x^2 + 7$  using Chebyshev's polynomials.