

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part. Use of non-programmable calculator is allowed.
x-x-x

1. (a) Find the relative error if a number is correct to n significant digits.
- (b) What is the difference between Transcendental and polynomial equation? Give examples also.
- (c) What is the difference between direct and iterative methods of solving simultaneous linear equations?
- (d) If λ is an eigen value of an orthogonal matrix A , then show that $1/\lambda$ is also its eigen value.
- (e) What is the difference between Newton interpolation and Hermite interpolation?
(5 × 2 = 10)

PART A

2. (a) Find the relative error if the number $x = 0.004997$ is
 - (i) Truncated to three decimal digits
 - (ii) rounded off to three decimal digits. (4)
- (b) Find a real root of the equation using bisection method correct to four decimal places: (6)

$$x^4 - x - 10 = 0$$

3. (a) Using Bairstow's method, obtain the quadratic factors of the following polynomial equation (upto third iteration) starting with $p_0 = 1$. (5)
 $q_0 = 0$:

$$x^4 - 8x^3 + 39x^2 - 62x + 50 = 0$$

- (b) Find a root of the equation $x^3 - 2x - 5 = 0$ using secant method correct to four decimal places.
4. (a) Apply Lagrange's formula inversely to obtain the root of the equation $f(x) = 0$, given that $f(30) = -30$, $f(34) = -13$, $f(38) = 3$ and $f(42) = 18$. (5)
- (b) Using Newton's forward interpolation formula, show that (5)

$$\sum n^3 = \left\{ \frac{n(n+1)}{2} \right\}^2$$

(2)

PART B

5. (a) Using Gauss- Jordan method, find the inverse of the matrix (5)

$$\begin{bmatrix} 2 & 2 & 3 \\ 2 & 1 & 1 \\ 1 & 3 & 5 \end{bmatrix}$$

- (b) Find the largest eigen-value and the corresponding eigen-vector of the matrix using power method: (5)

$$\begin{bmatrix} 1 & 3 & -1 \\ 3 & 2 & 4 \\ -1 & 4 & 10 \end{bmatrix}$$

6. Evaluate $\int_0^1 \frac{dx}{1+x}$ applying (10)

- (i) Trapezoidal rule
 (ii) Simpson's 1/3 rule
 (iii) Simpson's 3/8th rule.

7. (a) Using Euler's method, find approximate value of y when $x = 0.6$ of $\frac{dy}{dx} = 1 - 2xy$. given that $y(0) = 0$ (take $h = 0.2$). (5)

- (b) Find the best value of a and b such that $y = a + bx$ fits the given data in the table: (5)

x	0	1	2	3	4
y	1.0	2.9	4.8	6.7	8.6