

1079
M.E. (Mechanical Engineering)
Third Semester
MME-302(e): Optimization Techniques

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, selecting atleast two questions from each Section.

x-x-x

Question No.	SECTION-A	Marks																																								
1 (a)	Write in brief on historical development of optimization and mention a few applications of Optimization?	5																																								
(b)	A coal grassfire can use three grades of coal to produce quality K and M of producer gas. There are two processes (i.e. old and new) available to use the blended coal. For each production run the old process uses 10, 14 and 4 units of coal A, B and C to produce 12 units of K and 10 units of M. The new process uses 6, 18 and 8 units of coal A, B and C to produce 10 units of quality K and 14 units of M. Due to prior commitments, the gassi-fire plant must produce at least 1000 and 1600 units of K and M respectively for the next month. It has available 2000, 2500 and 1500 units of coal A, B and C respectively. For each unit of K a revenue of 3000 and for each unit of M, 4000 are received. Formulate this as LP problem so as to maximize the revenue.	5																																								
2	Solve the following LPP using simplex method. Max $Z = X_1 + 2x_2 + 3x_3$ S.T. $x_1 + 2x_2 + 3x_3 < 10$ $x_1, x_2 \leq 5$ $X_1 \leq 1, x_1, X_2 \geq 0$ Find the alternate optimal solution if it exists.	10																																								
3 (a)	Briefly explain about linear programming in two dimensional space.	5																																								
(b)	Briefly explain about standard form of a linear programming problem.	5																																								
4	Solve the following problem using Kuhn-tucker conditions: Maximize $f(x_1, x_2) = 2x_1 + x_2 - x_1^2$ Subject to $2x_1 + 3x_2 \leq 6$ $2x_1 + x_2 \leq 4$ $x_1, x_2 \geq 0$	10																																								
SECTION-B																																										
5	Find the optimal solution for the following transportation problem. The cell entries represent the unit transportation cost in rupees from each source to each destination.	10																																								
	<table border="1"> <thead> <tr> <th colspan="2"></th> <th colspan="5">To</th> <th>Supply</th> </tr> </thead> <tbody> <tr> <th rowspan="4">From</th> <td>3</td> <td>4</td> <td>6</td> <td>8</td> <td>9</td> <td>20</td> </tr> <tr> <td>2</td> <td>10</td> <td>1</td> <td>5</td> <td>8</td> <td>30</td> </tr> <tr> <td>7</td> <td>11</td> <td>20</td> <td>40</td> <td>3</td> <td>15</td> </tr> <tr> <td>2</td> <td>1</td> <td>9</td> <td>14</td> <td>16</td> <td>13</td> </tr> <tr> <td>Demand</td> <td>40</td> <td>6</td> <td>8</td> <td>18</td> <td>6</td> <td></td> </tr> </tbody> </table>			To					Supply	From	3	4	6	8	9	20	2	10	1	5	8	30	7	11	20	40	3	15	2	1	9	14	16	13	Demand	40	6	8	18	6		
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(2)

- 6 A truck can carry a total of 10 tonnes of product three types of products are available for shipment. Their weights & values are tabulated. Assuming that at least one each type must be shipped; determine the loading which will maximize the total value

Product type	Value (Rs)	Weight tonnes)
A	20	1
B	50	2
C	60	3

10

- 7 (a) A d.c generator has internal resistance of R ohms and develops an open circuit voltage of ' V ' volts. Find the value of load resistance ' r ' for which the power developed by generator will be maximum.

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- (b) What elementary operation can be used to transform
- $$2x_1 + x_2 + x_3 = 9$$
- $$x_1 + x_2 + x_3 = 6$$
- $$2x_1 + 3x_2 + x_3 = 13$$
- into
- $$x_1 = 3$$
- $$x_2 = 2$$
- $$x_1 + 3x_2 + x_3 = 13$$
- Find the solution of this system by reducing into canonical form.

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- 8 (a) Explain the computational procedure used in Dynamic programming.

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- (b) Write short notes on : (any two)
- (a) Population based Optimization techniques
- (b) Applications of Genetic Algorithm in optimization
- (c) Descent methods

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