

1079
B. Engg. (1st Year)-1st Semester
Bio Technology
APH-103: Quantum and Statistical Physics
(Common with IT and CSE)

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Q. No. 1 which is compulsory and selecting atleast two questions from each Part.

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- I. Attempt any five of the following:
- (a) Why the mass of the photon is considered to be zero in special theory of relativity?
 - (b) What was the failure of Galilean transformations?
 - (c) What are black holes? How can we detect them?
 - (d) What is the difference between continuous and characteristic X-rays?
 - (e) Why a particle cannot be at rest in the infinitely deep potential well?
 - (f) Under what circumstances, if any, is L_z equal to L ?
 - (g) What factors led to the introduction of spin quantum number?
 - (h) Calculate the number of different arrangements of 6 Bosons among 4 cells of equal a priori probability. (2x5 = 10)

Part A

- II. (a) Deduce the Einstein relativistic velocity addition theorem. Show that it is consistent with second postulate of relativity. (4)
- (b) A driver is caught going through red light. The driver claims to the judge that the colour she actually saw was green ($f = 5.60 \times 10^{14}$ Hz) and not red ($f_0 = 4.80 \times 10^{14}$ Hz) because of the Doppler effect. The judge accepts this explanation and instead fines her for speeding at the rate of Rs 1000 for each km/h she exceeded the limit of 100km/h. What was the total fine? (3)
- (c) Show that $(x^2 + y^2 + z^2 - c^2 t^2)$ is invariant under Lorentz transformation. (3)
- III. (a) What do you understand by Heisenberg Uncertainty Principle? Using this principle show that the electron cannot be a part of the nucleus. (4)
- (b) Derive an expression for the Compton shift. Find the maximum energy of the recoil electron. (6)
- IV. (a) Derive Schrodinger time independent wave equation. Will it be valid for relativistic particles? (6)
- (b) The wave function of a certain particle is $\psi = A \cos^2 x$ for $-\frac{\pi}{2} < x < \frac{\pi}{2}$. Find the value of A and also find the probability that the particle be found between $x=0$ and $x = \pi/4$. (4)

Part B

- V. (a) Show that the evenly spaced energy levels of quantum harmonic oscillator are given by equation: $E_n = \left(n + \frac{1}{2}\right) h\omega$ where n is quantum number. What is zero point energy? (6)
- (b) Show that the Pauli exclusion principle is a consequence of antisymmetric wave function? (4)
- VI. (a) Write the wave function for hydrogen atom. Discuss the significance of quantum numbers. (5)
- (c) How did Planck's hypothesis for black body radiation solve the ultraviolet catastrophe? (5)
- VII. (a) Show that the average kinetic energy of a three dimensional gas of N free electrons at 0°K is $\bar{E}_0 = \frac{3}{5} NE_F$. (5)
- (b) Compare Maxwell-Boltzmann, Bose-Einstein and Fermi-Dirac statistics. (5)

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