Special

Exam.Code:0906 Sub. Code: 6660

## 1108

## B.E. Second Semester MATHS-201: Differential Equations and Transformation

Time allowed: 3 Hours

Max. Marks: 50

**NOTE:** Attempt <u>five</u> questions in all, including Question No. I which is compulsory and selecting two questions from each Part. Use of non-programmable calculator is allowed.

x-x-x

- 1. (a) Define Dirac's Delta function and find its Laplace transform.
  - (b) Define even and odd functions and give examples.
  - (c) Find the partial differential equation by elimination arbitrary constants:  $z = (x a)^2 + (y b)^2 + 1$  where a, b are arbitrary constants.
  - (d) Solve the differential equation:  $(x-y)^2 \frac{dy}{dx} = a^2$ .
  - (e) Define Parseval's Identity and minimum square error in approximating a periodic function by a trigonometric polynomial of degree N. (5 × 2 = 10)

## PART A

2. (a) Solve the following differential equations:

(2.5+2.5)

(i) 
$$(x^4 + y^4)dx - xy^3dy = 0$$

(ii) 
$$\frac{dy}{dx} + y = e^{e^x}$$

(b) Find the general solution of the differential equation:

(5)

$$y'' - 2y' + y = x^2 e^{3x}$$

3. (a) Find the genral solution of the differential equation by method of variation of parameters: (5)

$$y'' - 2y' + y = 3x^{3/2}e^x$$

(b) Show that 
$$\int_{t-0}^{\infty} \int_{u=0}^{t} \frac{e^{-t} \sin(u)}{u} du \ dt = \pi/4$$
 (5)

4. (a) Find 
$$L(t^2u(t-1) + \delta(t-1))$$

(b) Find the Laplace Inverse of 
$$\cot^{-1}(s/2)$$
. (4)

(c) Find the inverse Laplace transform of 
$$\frac{e^{-1/\sqrt{s}}}{s}$$
. (2)

## PART B

5. (a) Is the given function even or odd? Find its Fourier series: (5)

$$f(x) = \begin{cases} \pi e^{-x} & \text{if } -\pi < x < 0 \\ \pi e^{x} & \text{if } 0 < x < \pi \end{cases}$$

(b) Find the Fourier sine and cosine integral representation of the function defined as: (5)

$$f(x) = \begin{cases} x & \text{if } 0 < x < 1\\ 0 & \text{if } x > 1 \end{cases}$$

6. (a) Find the equation of the integral surface of the differential equation: (7)

$$2y(z-3)p + (2x-z)q = y(2x-3)$$

which passes through the circle z = 0,  $x^2 + y^2 = 2x$ .

(b) Formulate the partial differential equation by eliminating arbitrary function: (3)

$$f(x^2 + y^2 + z^2, z^2 - 2xy) = 0$$

7. Find the D'Alembert's solution of one dimensional wave equation (L=length of the string with initial deflection f(x) and initial velocity g(x)) (10)

$$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}, \quad c^2 = T/\rho$$