

1058  
B.E. (Mechanical Engineering)  
Sixth Semester  
MEC-603: Mechanical Vibrations

Max. Marks: 50

Time allowed: 3 Hours

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part. Assume suitable data wherever necessary.

x-x-x

Question 1: Answer the following

- Define the number of degrees of freedom of a vibrating system.
- How do you add two harmonic motions having different frequencies?
- Suggest a method for determining the damping constant of a highly damped vibrating system that uses viscous damping.
- What assumptions are made in finding the natural frequency of a single-degree-of-freedom system using the energy method?
- What is critical damping, and what is its importance?

2 marks each=10 marks

Part A (All questions carry 10 marks each)

Question 2: Three springs and a mass are attached to a rigid, weightless bar PQ as shown in Fig. 1 2 Find the natural frequency of vibration and response of the system. Assume initial displacement as 'x' and initial velocity as 'v'.

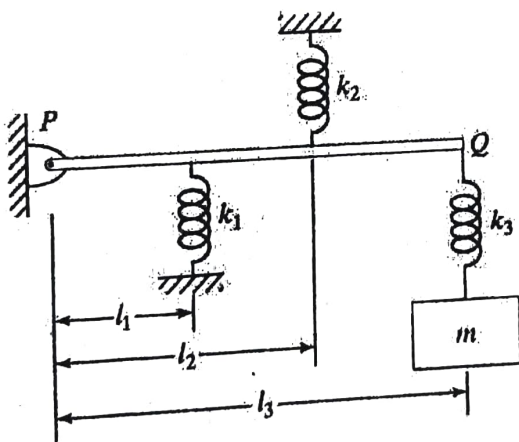


Fig. 1 (Question 2)

Question 3: Derive the equation of motion and find the steady-state response of the system shown in Fig. 2 for rotational motion about the hinge O for the following data:  $k = 5000 \text{ N/m}$ ,  $l = 1 \text{ m}$ ,  $c = 1000 \text{ N-s/m}$ ,  $m = 10 \text{ kg}$ ,  $M_0 = 100 \text{ N-m}$ , speed = 1000 rpm.

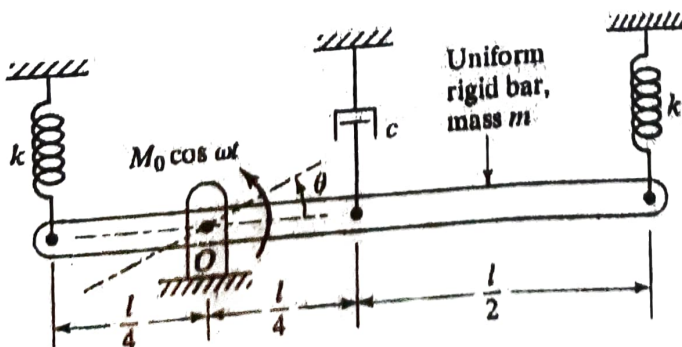


Fig. 2 (Question 3)

Question 4: Determine the steady-state response of the bar under a harmonic force, applied at the middle of the bar, as shown in the Fig. 3.

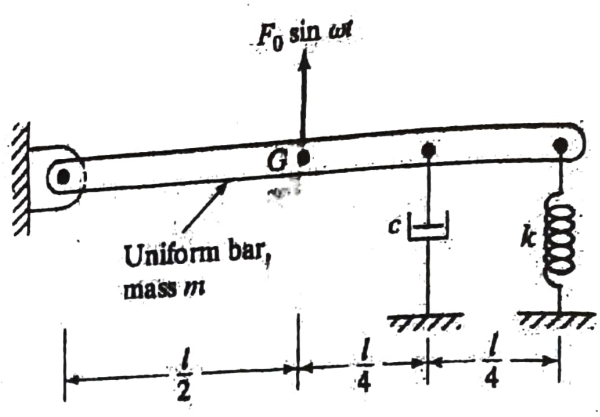


Fig. 3 (Question 4)

**Part B (All questions carry 10 marks each)**

Question 5: A two-mass system consists of a piston of mass  $m_1$ , connected by two elastic springs that moves inside a tube as shown in Fig. 4. A pendulum of length  $l$  and end mass  $m_2$  is connected to the piston. Derive the equations of motion of the system in terms of  $x_1(t)$  and  $u(t)$ . (b) Derive the equations of motion of the system in terms of the  $x_1(t)$  and  $x_2(t)$ . (c) Find the natural frequencies of vibration of the system.

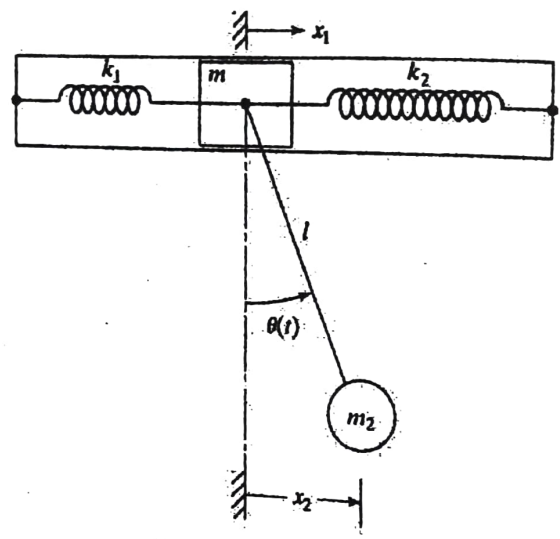


Fig 4 (Question 5)

Question 6: The mass matrix and eigen vectors of a vibrating system is given by

$$[m] = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \left\{ \begin{matrix} 1 \\ -1 \\ 1 \end{matrix} \right\}, \quad \left\{ \begin{matrix} 1 \\ 1 \\ 1 \end{matrix} \right\}, \quad \text{and} \quad \left\{ \begin{matrix} 0 \\ 1 \\ 2 \end{matrix} \right\}$$

Find the  $[m]$ -orthonormal modal matrix of the system.

Question 7: Derive equations of motion and solve the governing free vibration of a string with both ends fixed.